# All Digital Frequency Synthesizer Using A Flying Adder

Gang-Neng Sung, Szu-Chia Liao, Jian-Ming Huang, Yu-Cheng Lu, and Chua-Chin Wang<sup>†</sup>, Senior Member, IEEE,

Abstract—This article presents an all digital frequency synthesizer (ADFS) based on the flying adder architecture. The flying adder (FA) is a fascinating architecture for frequency synthesizer designs due to its simplicity and effectiveness. The FA-based frequency synthesizer can simply use a set of multiple phase reference signals to generate a desired frequency to achieve fast frequency switching. In the proposed work, the frequency synthesizer adopts an all-digital phase-locked loop (ADPLL) to provide a steady reference signal for the FA. The proposed frequency synthesizer is implemented in a standard 0.18  $\mu m$  CMOS cell-based technology and the core area is 0.16 mm<sup>2</sup>. The output frequency range is 39.38 MHz  $\sim$  226 MHz and the peak-to-peak jitter is less than 130 ps.

Index Terms-ADPLL, flying adder, CMOS, low power, ADFS

## I. INTRODUCTION

**T**HE frequency synthesizer is an essential component for many systems to generate a desired frequency for frequency conversion in RF transceivers or signal synchronization in SOC (system on chip) systems [1]. Therefore, a good frequency synthesizer design should meet the requirements of fast frequency switching and wide output frequency range. The most popular architecture of the existing solutions can be classified into PLL(phase-locked loop)-based frequency synthesizers and DDFSs (direct-digital frequency synthesizer). The PLL-based frequency synthesizers can easily generate high output frequency, but they usually suffer from an inherent inability to simultaneously provide both fast frequency switching and high spectral purity [2]. Besides, the wide tunable output frequency range is still a challenging topic in the PLL designs. DDFSs adopt mathematical manipulations to directly synthesize the output frequency, where the implementation can be realized by either the memory-based phase-to-sine mapping or an algorithm-based phase-to-sine conversion [3] - [11]. Due to the absence of the feedback loop and VCO (voltage-controlled oscillator), DDFSs can accomplish the fast frequency switching and the wide output range more easily compared to the PLL-based solutions. DDFSs are also able to maintain the continuous phase during the process of frequency switching. The main drawback of the DDFS is that they need a high resolution DAC (Digital-to-Analog Converter) to convert

the digital signals into an analog signal. Therefore, how to design a high speed and high resolution DAC becomes another difficult topic.

The flying adder architecture was firstly introduced in [13] to overcome the problem associated with the conventional frequency synthesizers. By exploiting a set of n reference signals with the same frequency but a multiphase clock, i.e., with a fixed phase step of 360 degrees/n, the flying adder can generate the output frequency up to n/2 times of the reference frequency [12]. Notably, this architecture can generate a high output frequency using low frequency reference signals, which is a favorably effective and cost-efficient scheme for the demand for high speed clock generation in the modern SOCs. Prior works, [13] - [17], adopted the PLL to provide the reference signals. However, the traditional PLL design parameters of mixed-signal circuits seriously depend upon CMOS technology, which results in a poor reusability, particularly in the trend of the scaling down of the CMOS technology. This paper presents an all digital frequency synthesizer (ADFS) based on the flying adder architecture, where the reference signals is supplied by an all-digital PLL (ADPLL).

## II. All Digital Frequency Synthesizer Architecture

Fig. 1 shows the block diagram of the proposed all digital frequency synthesizer architecture. The ADPLL [18] - [22] is employed to track the phase of the reference clock,  $CLK_IN$ , and generate a phase-locked clock signal,  $OUT\_CLK$ , to the delay chain block. The delay chain produce 32 reference signals with an equal phase difference. The flying adder uses the multiple phase reference signals to synthesize the desired frequency according to the frequency control word, FCW. The details of each function block in Fig. 1 are described as follows.



Fig. 1. The block diagram of the proposed all digital frequency synthesizer.

#### A. All-digital phase-locked loop

The detailed block diagram of the ADPLL is shown in Fig. 2, where the ADPLL is composed of a phase frequency detector (PFD), a frequency divider (FDIV), two digital-controlled

This research was partially supported by Ministry of Economic Affairs, Taiwan, under grant 98-EC-17-A-02-S2-0017, 98-EC-17-A-07-S2-0010, 98-EC-17-A-01-S1-104, 98-EC-17-A-19-S1-133, National Health Research Institutes under grant NHRI-EX98-9732EI, and National Science Council under grant NSC 96-2923-E-110-001-MY3.

<sup>&</sup>lt;sup>†</sup>Prof. C.-C. Wang is the contact author. (email: ccwang@ee.nsysu.edu.tw) All of the authors are with Department of Electrical Engineering, National Sun Yat-Sen University, 80424, Taiwan.



Fig. 2. Block diagram of the ADPLL.

oscillators (FB\_DCO and OUT\_DCO), and a phase searching controller (PSC). PFD detects the phase difference between the reference clock  $CLK_IN$  and the feedback clock  $CLK_FB$ . When  $CLK_FB$  lags  $CLK_IN$ , PFD generates a negative impulse on UP, while DOWN remains at high to inform PSC to speed up the FB\_DCO. On the contrary, a negative impulse on DOWN is generated to slow down FB\_DCO if  $CLK_FB$  leads  $CLK_IN$ . The PSC generates two signals, COARSE and FINE, for FB\_DCO to select an oscillating frequency of the multiplied clock signal in feedback loop,  $CLK_FB_M$ . The frequency of  $CLK_FB_M$  is divided by FDIV to generate the divided signal  $CLK_FB$  which is sent back to PFD.

If the phase of the *CLK\_IN* is clocked, a signal *LOCK* is generated by PSC to indicate that the frequency is locked successfully. To further reduce the jitter caused by deadzone of the PFD and the finite resolution of FB\_DCO, the PSC computes the averaged values of *COARSE* and *FINE*, i.e., *AVG\_COARSE* and *AVG\_FINE*, respectively, for OUT\_DCO to generate the stable output signal *OUT\_CLK*. The PSC uses a binary search scheme, as shown in Fig. 3 to control the DCOs to generate the oscillating frequency with desired phases for the locking process.



Fig. 3. The binary search for the target frequency [22].

Referring to Fig. 2, there are two DCOs, FB\_DCO and OUT\_DCO. The FB\_DCO is located at the feedback loop, which is employed to lock the phase of the reference signal, and the OUT\_DCO generates the output signal when the phase

is locked. Fig. 4 shows the block diagram of the FB\_DCO. The control words, COARSE and FINE, select the appropriate delay cells of the COARSE-TUNE and FINE-TUNE blocks, respectively, to generate the desired oscillating frequency. The operation of the OUT\_DCO is similar to the FB\_DCO. In [23], the tri-state buffers were used to switch the delay cells. However, using the tri-state buffer might cause timing violations. The reason is that the "high-Z" state caused by the tri-state buffers will be fed back to feedback loop of the ADPLL when the control signals to switch tri-state buffers do not arrive at the same time. As a result, it will cause the timing harzad during the locking process. Instead, we adopt multiplexers to switch the delay cells to resolve this problem. Additionally, a rising edge of the input signal of the multiplexer is pre-set to wait for COARSE and FINE signals and then switch the delay line such that the timing violation can be avoided.

### B. Delay Chain

If the ADPLL successfully locks the phase of the reference clock,  $CLK_IN$ , the output of the ADPLL is passed to the delay chain to generate the multiple phase signals for the flying adder. The delay chain is composed of a series of the buffer cells as shown in the Fig. 5(a). Fig. 5(b) depicts the resultant reference signals, where  $\triangle$  is the propagation delay of each buffer. A larger number of the resultant reference signals gives a finer frequency resolution. The number of the buffers is 32 in our design. For instance, if we need 120 MHz as the ADPLL output frequency,  $\triangle$  should be 0.2625 ns. Therefore, the delay chain in the proposed design preferably consists of 32 buffers with a 0.2625 ns propagation delay.

#### C. Flying Adder

The flying adder architecture is adopted in the proposed frequency synthesizer. Fig. 6 shows the block diagram of the flying adder [14], where the PART\_A and PART\_B are similar circuits, where the major difference between these two function blocks is the size of the adders. Referring to PART\_B, when CLK2 is high, the summation of ADD\_1 and reg\_1 is stored in the reg\_2, and the value previously stored in the reg\_2 is passed to a 32-to-1 multiplexer, MUX1, to select one of the delay chain output signals, DCO[31:0], as the input signal of the 2-to-1 multiplexer, MUX3. The



Fig. 4. The block diagram of the FB\_DCO.



Fig. 5. (a) The schematic of the delay chain. (b) The resultant multiple phase reference signals.

accumulation step in PART\_B is determined by the frequency control word, FCW1. The operation of the PART\_A is similar to the PART\_B except that the reg\_4 is triggered by CLK1. Therefore, MUX3 always selects the signal generated at last half clock cycle, which can avoid the glitch caused by the transition of the input signal propagating through the MUXs. Eliminating the glitch can prevent the D-type flip-flop (DFF) from being triggered by false signals.

The desired frequency is synthesized by triggering the DFF with the signal selected from DCO. The relation between the frequency control word, FCW, and the desired frequency,

 $f_{out}$  can be expressed as follows:

$$\frac{1}{f_{out}} = \frac{T_{DCO}}{N} \times FCW,\tag{1}$$

where  $T_{DCO}$  is the period of the *DCO* signals, and *N* is the number of the *DCO* signals [24]. For example, to obtain an output frequency of 150 MHz given that the number and the frequency of the *DCO* signals are 32 and 150 MHz, respectively, the required *FCW* is around 25.371=(011001.01011)<sub>2</sub>. The longer length of the *FCW*'s decimal part results in a finer frequency resolution. The length of the *FCW* in the proposed frequency synthesizer is 11 bits, where *FCW*[10:5] and *FCW*[4:0] represent the integer part and the decimal part, respectively.

## III. IMPLEMENTATION AND MEASUREMENT

The proposed ADFS is carried out by the standard 0.18  $\mu$ m CMOS technology to verify the performance. All of the process corners : [0°C, +100°C], and (SS, TT, FF) models, are simulated. Fig. 7 shows the waveform of the synthesized frequency. Referring to Fig. 7(a), when the phase of  $CLK_IN$  is locked, the ADPLL generates a 80 MHz clock signal,  $OUT\_CLK$ , and the synthesized frequency, CLKI is changed from 39.38 MHz to 170 MHz according to the change of the FCW, where the frequency switching latency is two CLKI cycle. Fig. 7(b) shows a part of the multiple phase reference signals produced by the delay chain.

Fig. 8 shows the die photo of the proposed frequency synthesizer. Fig. 9 reveals that when the frequency of the ADPLL clock signal is locked, where the locked frequency is 187.5 MHz, the 3rd harmonic frequency is 570 MHz. At the same locked frequency, the voltage and time of the



Fig. 6. The Flying Adder.

eye diagram depicted in Fig. 10 are 1.31 V and 2.43 ns, respectively. Referring to Fig. 11, which is a measurement result on Agilent SOC 93000, *CLK1* varies from 80 MHz to 40 MHz when FCW is updated. It takes only four  $OUT\_CLK$  cycles to re-lock. The performance comparisons of our design and several prior works are summarized in Table I. The proposed ADFS attains the edge of low power and short lock time (cycles).

## IV. CONCLUSION

The flying adder architecture was developed to resolve challenges encountered in the design of the conventional PLL-based frequency synthesizer. Although the flying adder architecture only needs a simple PLL to provide multi-phased signals, the integration of the mixed-signal circuits still needs efforts on both the design and the simulation stages. Besides, analog circuits are much more sensitive to the variation of the technology compared to the digital circuits. In this paper, we propose an all digital frequency synthesizer based on the flying adder architecture, where the mixed-signal PLL is replaced with a low-power ADPLL. Moreover, the glitch hazard on both the flying adder and the ADPLL is eliminated to ensure the stability of the frequency synthesizer.

TABLE I PERFORMANCE COMPARISONS WITH SEVERAL PRIOR WORKS

ADPLL	[25]	[26]	[18]	[27]	Ours
Process (µm)	0.18	0.18	0.18	0.18	0.18
Year	2005	2008	2009	2009	2009
Maximum					
Frequency (MHz)	1500	725	250	560	226
Minimum					
Frequency (MHz)	520	70	87	53	39.38
Supply					
Voltage (V)	1.8	1.8	0.9	N/A	1.8
Maximum Lock					
Time (cycles)	$\leq 96$	$\leq$ 72	$\leq 72$	N/A	$\leq 4$
Jitter (ps)	76	N/A	152	51	130
Power					
Dissipation (mW)	26.8	27	5.4	25.2	3.6
Area (mm <sup>2</sup> )	0.27	0.174	0.76	0.14	0.16



Fig. 7. The waveform of the generated output signal: (a) the output frequency is changed from 39.38 MHz to 170 MHz; (b) multiple phase reference signals generated by the delay chain.



Fig. 8. The die photo of the proposed frequency synthesizer.



Fig. 9. The waveform of the output frequency locked on 187.5 MHz.



Fig. 10. The eye diagram for the output synthesized frequency, where locked frequency is 187.5 MHz.

OUT_CLK			
RESET		← →	
FCW	80 MHz	switch time	40 MHz

Fig. 11. The waveform of the output frequency switching from 80 MHz to 40 MHz.

#### ACKNOWLEDGEMENT

The authors would like to express their deepest gratefulness to CIC (Chip Implementation Center) of NARL (National Applied Research Laboratories), Taiwan, for their thoughtful chip fabrication service.

#### REFERENCES

- R. Best, Phase-Locked Loops: Design, Simulation, and Application, McGraw-Hill, 2003.
- [2] A. Yamagishi, M. Ishikawa, T. Tsukahara, and S. Date, "A 2-V, 2-GHz low-power direct digital frequency synthesizer chip-set for wireless communication," *IEEE J. Solid-State Circuits*, vol. 33, no. 2, pp. 210-217, Feb. 1998.
- [3] J. Vankka, K. Halonen, Direct Digital Synthesizers: Theory, Design and Applications, Springer 2006.
- [4] A. M. Sodagar and G. R. Lahihi, "A novel architecture for ROM-less sin-output direct digital frequency synthesizers by using the 2nd-order parabolic approximation," *IEEE/EIA Inter. Frequency Control Symp. and Exhibition*, pp. 284-289, June 2000.

- [5] A. Ashrafi and R. Adhami, "A 13-Bit resolution ROM-less direct digital frequency synthesizer based on a trigonometric quadruple angle formula," *IEEE Transactions on Very Large Scale Integration (VLSI) Syst.*, Vol. 13, No. 9, pp. 1096-1098, Sept. 2005.
- [6] H. Jafari, A. Ayatollahi, and S. Mirzakuchaki. "A low power, high SFDR, ROM-less direct digital frequency synthesizer," in *Proc. of 2005 IEEE Conference on Electron Devices and Solid-State Circuits*, Dec. 2005.
- [7] C.-C. Wang, J.-M. Huang, Y.-L. Tseng, W.-J. Lin, and R. Hu, "Phaseadjustable pipelining ROM-less direct digital frequency synthesizer with a 41.66-MHz output frequency," *IEEE Trans. Circuits Syst. II Exp. Briefs*, vol. 53, no. 10, pp. 1143-1147, Oct. 2006.
- [8] A. Ashrafi and R. Adhami, "An optimized direct digital frequency synthesizer based on even fourth order polynomial interpolation," in *Proc. 38th IEEE Southeastern Symposium on System Theory*, pp. 109-113, Mar. 2006.
- [9] D. De Caro and A. G. M. Strollo, "High-performance direct digital frequency synthesizers in 0.25 μm CMOS using dual-slope approximation," *IEEE J. Solid-State Circuits*, vol. 40, no 11, pp. 2220-2227, Nov. 2005.
- [10] B. Izouggaghen, A. Khouas, and Y. Savaria, "Spurs modeling in direct digital period synthesizers related to phase accumulator truncation" *IEEE International Symposium on Circuits and Systems 2004 (ISCAS* '04), Vol. 3, pp. 389-392, May 2004.
- [11] B. Pontikakis, H.-T. Bui, F-R. Boyer, Y. Savaria, "Precise free-running period synthesizer (FRPS) with process and temperature compensation," *IEEE MidWest Symposium on Circuits and Systems 2007 (MWSCAS* '07), pp. 1118-1121, Aug. 2007.
- [12] P. Sotiriadis, "Timing and spectral properties of the Flying Adder frequency synthesizers," *IEEE International Frequency Control Symposium* 2009, pp. 788-792, July 2009.
- [13] H. Mair and L. Xiu, "An architecture of high-performance frequency and phase synthesis," *IEEE J. Solid-State Circuits*, vol. 35, no. 6, pp. 835-846, Jun. 2000.
- [14] L. Xiu and Z. You, "A flying-adder architecture of frequency and phase synthesis with scalability," *IEEE Trans. VLSI syst.*, vol. 10, no. 5, pp.637-649, Oct. 2002.
- [15] L. Xiu and Z. You, "New frequency synthesis method based on Flying-Adder architecture," *IEEE Trans. on Circuits and Systems II: Analog* and Digital Signal Processing, vol. 50, no. 3, pp. 130-134, March 2003.
- [16] P. Sotiriadis, "Intrinsic Jitter of Flying-Adder Frequency Synthesizers", *IEEE International Sarnoff Symposium 2009*, pp. 1-4.
- [17] L. Xiu, "A "Flying-Adder" on-chip frequency generator for complex SoC environment " IEEE Trans. on Circuits and Systems II: Express Briefs, vol. 54, no. 12, 2007.
- [18] Y.-M. Chung and C.-L. Wei, "An all-digital phase-locked loop for digital power management integrated chips," *IEEE Int. Circuits Syst. Symp.*, pp. 2413-2416, May 2009.
- [19] J.-S. Chiang and K.-Y Chen, "The design of an all-digital phase-locked loop with small DCO hardware and fast phase lock," *IEEE Trans. Circuits Syst. II*, vol. 46, no. 7, pp. 945-950, July 1999.
- [20] T. Olsson and P. Nilsson, "An all-digital PLL clock multiplier," in Proc. of 2002 IEEE Asia-Pacific Conference on ASICs, Taiwan, pp. 275-278, 2002.
- [21] T. Olsson and P. Nilsson, "A digitally controlled PLL for SoC applications," *IEEE J. Solid-State Circuits*, vol. 39, no. 5, pp. 751-760, May 2004.
- [22] C.-C. Wang, C.-C. Huang, and S.-L. Tseng, "A low-power ADPLL using feedback DCO quarterly disabled in time domain," *Microelectronics Journal*, vol. 39, no. 5, pp. 832-840, May 2008.
- [23] C.-C. Chung and C.-Y Lee, "An all-digital phase-locked loop for highspeed clock generation," *IEEE J. Solid-State Circuits*, vol. 38, no. 2, pp. 347-351, Feb. 2003.
- [24] L. Xiu, "The concept of time-average-frequency and mathematical analysis of Flying-Adder frequency synthesis architecture," *IEEE Circuits* and Systems Magazine, vol. 8, no. 3, pp. 27-51, Sep. 2008.
- [25] K.-J. Lee, S.-H. Jung, Y.-J. Kim, C. Kim, and S. Kim, "A digitally controlled oscillator for low jitter all digital phase locked loops," *IEEE Solid-State Circuits Conference*, pp. 365-368, Nov. 2005.
- [26] H.-J. Hsu, C.-C. Tu, and S.-Y. Huang, "A high-resolution all-digital phase-locked loop with its application to built-in speed grading for memory," *Proc. of Intl Symp. on VLSI Design, Automation and Test*, pp. 267-270, Apr. 2008.
- [27] H.-J. Hsu, S.-Y. Huang, "A low-jitter all-digital phase-locked loop using a suppressive digital loop filter," *Proc. of Intl Symp. on VLSI Design, Automation and test*, (VLSI-DAT'09) pp. 158-161, Apr. 2009.