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Analysis of Layout Arrangement for CMOS Oscillators to Reduce Overall Variation on Silicon

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ABSTRACT
This investigation demonstrates the analysis of various layout arrangements for oscillator (OSC) realized by CMOS technologies. Moreover, the analysis reveals that the serpentine style of OSC stages attains the minimum output variation on silicon. This investigation is firstly verified by post-layout simulations, comparing the variation with different kinds of layout arrangement for OSC designs, including samparting layout style, straight layout style, and
staggered layout style, etc. The proposed design is then realized using $0.18 \ \mu m$ process to justify
the performance, where a straight line layout style and a serpentine layout style of OSC are
physically fabricated on the same die. Besides, the on-silicon measurement is conducted to give
the comparison for these two different styles of OSC designs. The proposed serpentine layout
style attains the lowest layout variation when the variations are not homogeneous in different
directions on the same silicon plane.

1 Introduction

Thanks to the advancement of CMOS semiconductor technologies, transistors as well as other passive devices are downsized constantly and rapidly. Under the continuous shrinking of nanometer manufacturing process, 180 nm, 90 nm, 40 nm, 28 nm, and even 16 nm, manufacturing variations on wafer become a serious threat to the functionality of logic devices. However, The reason is no matter what process is used, it is suffered from various environmental factors [1]-[14], e.g., voltage, temperature, power surge, process variations, etc. In addition to the environmental factors, the impact of the layout parasitic and arrangement is also an important issue for IC design [15]-[17]. Oscillator (OSC) is one of the major components of digital circuits, which is usually used as the clock generator.

2 Literature Survey

This investigation explores what kind of layout arrangement of OSCs composed of many identical delay stages will attains the best robustness to the variations caused by manufacturing on wafers. The theoretical analysis was verified not only by simulation results, but also physical measurement. In prior works, the measurement results were much worse than the post-layout simulation results mainly due to lack of layout style analysis [18]-[20], and the worst frequency drift is about 0.2 GHz from 1 GHz-3 GHz in these works. Notably, many prior digital circuit design reports never gave details of their clock or OSC generator layout, e.g., [21]-[24]. To keep the simulation conditions consistent for different layout arrangement of OSCs, all OSCs are realized using the same 64 inverters for various 8×8 and 1×64 combinations in this investigation. Besides, to verify as many possibilities as possible, this investigation demonstrates the analysis of 7 layout arrangements of OSCs by post-layout simulations with full RC extract and Monte Carlo simulation results. Though the layout arrangements look similar for 7 layout arrangements of OSCs, the wiring length between buffers in these cases are not identical. This investigation analytically computes the overall wiring length to predict the RC impact and the variation effect in the different layout styles.

3 Layout Variation Analysis of Oscillator Designs

Figure 1 shows the architecture of a typical differential oscillator. It consists of a Driving Buffer, two 64-to-1 MUX arrays, 64 delay stages, and a Decoder to select the desired frequency. Although

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Figure 1: The architecture of the illustrative OSC with 64 delay stages

voltage variation, temperature variation, and process variation are usually considered by chip designers, there are still other variations caused by layout styles. Typical process variation on wafer are usually caused by the non-uniform and linearly degradation doping concentrations of chemical substances. Assume that the variation, $P_A(0,0)$, at the origin A(0,0) has the minimum variation c. We then define the variation amount along the x axis for each buffer stage is "a", and the variation along y axis is "b" without the loss of robustness. In other words, the variation is assumed to be a linear function against the distance. And the variation amount is different in different directions on the same die (plane). For example: B(i,j)delay stage has variation $P_B(i,j)$ as follows.

$$P_{B}(i,j) = a \cdot i + b \cdot j + c \tag{1}$$

• In the case of a straight line arrangement layout of OSC in Figure 2, the total variation P_{total1}(i, j) is found as:

$$\sum_{i=1}^{64} \sum_{j=1}^{1} P_{total1}(i, j)$$

=
$$\sum_{i=1}^{64} \sum_{j=1}^{1} (a \cdot i + b \cdot j + c)$$

=
$$2080 \cdot a + 64 \cdot b + 64 \cdot c$$
 (2)

Average of variation $P_{totalaverage1}(i, j)$ is:

$$P_{\text{totalaverage1}}(i, j) = 32.5 \cdot a + b + c \tag{3}$$

buf1 buf2 buf3 buf4 ----- buf61 buf62 buf63 buf64

Figure 2: Straight line layout style of OSC

Notably, buf# (# = 1-64) stands for inverter-based buffers.

• In Figure 3, in the case of a serpentine layout style of OSC, the total variation P_{total2}(i, j) is:

$$\sum_{i=1}^{8} \sum_{j=1}^{8} P_{\text{total2}}(i, j)$$

= $\sum_{i=1}^{8} \sum_{j=1}^{8} (a \cdot i + b \cdot j + c)$
= 288 \cdot a + 288 \cdot b + 64 \cdot c (4)

Average of variation Ptotalaverage2(i, j) is:

$$P_{\text{totalaverage2}}(i,j) = 4.5 \cdot a + 4.5 \cdot b + c \tag{5}$$

Σ	buf1	buf2	buf3	buf4	buf5	buf6	buf7	buf8	
Γ.	buf16	buf15	buf14	buf13	buf12	buf11	buf10	buf9	Ľ
Ľ	buf17	buf18	buf19	buf20	buf21	buf22	buf23	buf24	
	buf32	buf31	buf30	buf29	buf28	buf27	buf26	buf25	
	buf33	buf34	buf35	buf36	buf37	buf38	buf39	buf40	
	buf41	buf42	buf43	buf44	buf45	buf46	buf47	buf48	
	buf56	buf55	buf54	buf53	buf52	buf51	buf50	buf49	
	buf57	buf58	buf59	buf60	buf61	buf62	buf63	buf64	

Figure 3: Serpentine layout style of OSC

Based on Eqn. (2) and (4), we make a conclusive derivation as follows.

$$P_{\text{total1}}(\mathbf{i}, \mathbf{j}) \ge P_{\text{total2}}(\mathbf{i}, \mathbf{j})$$
$$\Rightarrow 2080 \cdot a + 64 \cdot b + 64 \cdot c \ge 288 \cdot a + 288 \cdot b + 64 \cdot c \qquad (6)$$

 $\Rightarrow 8 \cdot a \ge b$

Thus, the variation of the serpentine style is better than straight arrangement when "a" is more than or equal to one eighth of "b". This implies that if the variations in different directions are not equal, the serpentine layout style attains the better resistance to overall variations on wafer. This fact was never reported before in any prior work analytically. Notably, the similar analytic approach is applied to other layout styles as those described in the following text.

Results and Discussion 4

4.1Simulation and Verification

buf1

buf31

buf33

buf63

buf64 buf48

buf18

buf16

In order to verify as many possibilities as possible before physical realization on silicon, this investigation demonstrates 7 layout

arrangements of OSCs as shown in Figure 4, where various arrangements and post-layout simulations with RC extract of OSCs are demonstrated. Given that the central frequency of a 64-stage OSC is 100 MHz by pre-layout simulations, it is assumed that the parasitic variation is ignored. A total of 7 different layout arrangements are shown in Figure 4, namely A, B, C, D, E, F, and G. These styles are briefly described as follows.

- A. common centroid + even-odd stage interleaved
- B. common centroid in 2 directions diagonally
- C. circle to the center
- D. serpentine
- E. line by line
- F. 2-line circle to the center
- G. straight line

The post-layout simulation of serpentine layout style shows the closest result to 100 MHz. Besides, the error between the serpentine layout style and pre-layout simulation is only 1.9%. In short, the serpentine layout style is the best arrangement proved by this post-layout simulation result.

Because of the limit of chip size and budget, we are only allowed to carry out the serpentine layout style and straight layout style on

A. t	53.	6	V	HZ

B. 72 MHz

C. 95.3 MHz

buf3	buf5	buf7	buf9	buf11	buf13	buf15	buf1	buf5	buf9	buf13	buf17	buf21	buf25	buf4		buf1	buf2	buf3	buf4	buf5	buf6	buf7	buf8
buf29	buf27	buf25	buf23	buf21	buf19	buf17	buf27	buf29	buf33	buf37	buf41	buf45	buf32	buf8		buf28	buf29	buf30	buf31	buf32	buf33	buf34	buf9
buf35	buf37	buf39	buf41	buf43	buf45	buf47	buf23	buf47	buf49	buf53	buf41	buf52	buf36	buf12		buf27	buf48	buf49	buf50	buf51	buf52	buf35	buf10
buf61	buf59	buf57	buf55	buf53	buf51	buf49	buf19	buf43	buf59	buf61	buf64	buf56	buf40	buf16	I	buf26	buf47	buf60	buf61	buf62	buf53	buf36	buf11
buf62	buf60	buf58	buf56	buf54	buf52	buf50	buf15	buf39	buf55	buf63	buf62	buf60	buf44	buf20		buf25	buf46	buf59	buf64	buf63	buf54	buf37	buf12
buf46	buf44	buf42	buf40	buf38	buf36	buf34	buf11	buf35	buf51	buf42	buf54	buf50	buf48	buf24		buf24	buf45	buf58	buf57	buf56	buf55	buf38	buf13
buf20	buf22	buf24	buf26	buf28	buf30	buf32	buf7	buf31	buf46	buf42	buf38	buf34	buf30	buf28		buf23	buf44	buf43	buf42	buf41	buf40	buf39	buf14
buf14	buf12	buf10	buf8	buf6	buf4	buf2	buf3	buf28	buf22	buf18	buf14	buf10	buf6	buf2		buf22	buf21	buf20	buf19	buf18	buf17	buf16	buf15

10.6 x 45.81 um

D. 98.1 MHz

buf1	buf2	buf3	buf4	buf5	buf6	buf7	buf8
buf16	buf15	buf14	buf13	buf12	buf11	buf10	buf9
buf17	buf18	buf19	buf20	buf21	buf22	buf23	buf24
buf32	buf31	buf30	buf29	buf28	buf27	buf26	buf25
buf33	buf34	buf35	buf36	buf37	buf38	buf39	buf40
buf41	buf42	buf43	buf44	buf45	buf46	buf47	buf48
buf56	buf55	buf54	buf53	buf52	buf51	buf50	buf49
buf57	buf58	buf59	buf60	buf61	buf62	buf63	buf64

10.6 x 40.8 um

E. 96.7 MHz

12.01 x 44.66 um

buf1	buf2	buf3	buf4	buf5	buf6	buf7	buf8
buf9	buf10	buf11	buf12	buf13	buf14	buf15	buf16
buf17	buf18	buf19	buf20	buf21	buf22	buf23	buf24
buf25	buf26	buf27	buf28	buf29	buf30	buf31	buf32
buf33	buf34	buf35	buf36	buf37	buf38	buf39	buf40
buf41	buf42	buf43	buf44	buf45	buf46	buf47	buf48
buf49	buf50	buf51	buf52	buf53	buf54	buf55	buf56
buf57	buf58	buf59	buf60	buf61	buf62	buf63	buf64

F. 97.3 MHz

10.6 x 40.8 um

buf1	buf4	buf5	buf8	buf9	buf12	buf13	buf14
buf2	buf3	buf6	buf7	buf10	buf11	buf16	buf15
buf47	buf48	buf49	buf52	buf53	buf54	buf17	buf18
buf46	buf45	buf50	buf51	buf56	buf55	buf20	buf19
buf43	buf44	buf63	buf62	buf57	buf58	buf21	buf22
buf42	buf41	buf64	buf61	buf60	buf59	buf24	buf23
buf39	buf40	buf35	buf34	buf31	buf30	buf25	buf26
buf38	buf37	buf36	buf33	buf32	buf29	buf28	buf27

10.6 x 40.8 um

10.6 x 40.8 um

buf61 buf62 buf63 buf64 buf1 buf2 buf3 buf4 G. 89.2 MHz 38.5 x 10.75 um

Figure 4: Various arrangements and the clock rates of OSC by post-layout simulations



Figure 5: (a) The Monte Carlo simulation histogram of serpentine layout style of OSC; (b) The Monte Carlo simulation histogram of straight line layout style of OSC (MC times=1000)

	MWCL[21]	VLSI[22]	JSSC[23]	JSSC[24]	this w	ork
Year	2017	2019	2019	2021	2022	
VDD (V)	1	0.8	1.2	1	3.3	
Layout arrangement	straight	straight	straight	straight	serpentine	straight
Layout variation	N/A	N/A	N/A	N/A	Yes	
Accuracy	N/A	N/A	N/A	N/A	95.5%	88.7%
Frequency range	1 MHz	3.2 GHz-4 GHz	2.1 GHz-3.1 GHz	3.6 GHz-3.6175 GHz	20 MHz-180 MHz	
Bandwidth	10 MHz	10 MHz	10 MHz	100 MHz	100 MHz	
Adjustable frequency	Yes	Yes	Yes	Yes	Yes	3
Chip Area (mm ²)	0.75	1	0.25	0.00525	1.3	
Chip Area						
(Normalization) 1.775		2.36	0.6	0.108	0.4	
(10^{-4} mm^2)						
FOM	8.8	2820	11888	15700	12100, 2	3606 [∆]

Table 1	1:	Comparison	with	prior	works

 $FOM = \left(\frac{\text{Frequency range} \cdot \text{Bandwidth}}{\text{VDD} \cdot \text{Normalized Chip Area}}\right)$

 $^{\Delta}$ This FOM is counted only by the area of the serpentine style.

silicon. Their areas are $10.6 \times 40.8 \,\mu\text{m}^2$ (serpentine) and $38.5 \times 10.75 \,\mu\text{m}^2$ (straight line), respectively. Figure 5 shows the Monte Carlo simulation results of two different layout styles to verify the reliability, respectively. As shown in Figure 5, the central frequency of serpentine layout style is closer to 100 MHz, which is set to be the central frequency of this investigation.





Figure 7: The enlarged layout style of OSC (a) serpentine style; (b) straight line style

4.2 Measurement and Performance Comparison

To verify the previous analysis, the proposed OSC designs are realized using TSMC 180 nm CMOS process. The layout and die photo of the OSCs are shown in Figure 6 (a) and (b), respectively, where the total chip area is $1.063 \times 1.063 \text{ mm}^2$, and the core area is $989 \times 344 \mu\text{m}^2$. Notably, there are 2 OSC designs (straight line,



Figure 6: (a) OSC layout; (b) OSC die photo



Figure 8: Measurement setup and equipment

serpentine) on the same die. The detailed layouts of the mentioned OSCs are enlarged in Figure 7. To highlight the influences from the different layout styles, the space between any two adjacent stages in Figure 7 is the same. The chip measurement setup is shown in Figure 8. The chip is soldered on the PCB to reduce noise interference. The Agilent E3631A Power Supply provides the required voltages and enable signals to the chip. Arbitrary waveform generator Agilent 33522A provide the 6-bit selection code. The oscilloscope WaveRunner610Zi is used to observe waveforms and monitor the circuit operations.

	95.5 MHZ											
buf1	buf2	buf3	buf4	buf5	buf6	buf7	buf8					
buf16	buf15	buf14	buf13	buf12	buf11	buf10	buf9					
buf17	buf18	buf19	buf20	buf21	buf22	buf23	buf24					
buf32	buf31	buf30	buf29	buf28	buf27	buf26	buf25					
buf33	buf34	buf35	buf36	buf37	buf38	buf39	buf40					
buf41	buf42	buf43	buf44	buf45	buf46	buf47	buf48					
buf56	buf55	buf54	buf53	buf52	buf51	buf50	buf49					
buf57	buf58	buf59	buf60	buf61	buf62	buf63	buf64					

10.6 x 40.8 um (a) The block diagram of serpentine layout style of OSC



respectively. By comparing the pre-layout simulation (100 MHz) with the measurement results, the deviations of serpentine layout style and straight line layout style of OSCs are 4.5% and 11.3%, respectively.



Figure 10: (a) The measurement waveform of central frequency of serpentine layout style; (b) The measurement waveform of central frequency of straight layout style

To verify the selectability of OSCs, Figure 11 shows the comparison of pre-layout simulation, post-layout simulation, and the chip measurement results by different selection codes (1-15). The

Figure 9: (a) The block diagram of serpentine layout style of OSC; (b) The block diagram of straight line layout style of OSC

Figure 9 shows the block diagrams of serpentine layout style and straight line layout style of OSCs in Figure 6 and 7. Figure 10 (a), (b) show the measurement waveforms of these 2 layout styles,



Figure 11: Comparison of pre-layout simulation, post-layout simulation, and the chip measurement results



Figure 12: (a) The all chip measurement results of serpentine layout style of OSC by all different selection codes; (b) The all chip measurement results of straight line layout style of OSC by all different selection codes

measurement result of the serpentine layout style is closer to the prediction of post-layout simulations. To justify the repeatability of the chip measurement, all 6 chips are measured with 10 times and the results are shown in Figure 12. The average error of the serpentine style layout is smaller than that of the straight line counterpart. Table 1 tabulates the performance comparison of the proposed design and several recent works about layout arrangement. The proposed design achieves the second best FOM because our chip contains two layout arrangements of OSCs. In other words, the chip consumes much larger area than others. Notably, the proposed design would have the best FOM if only the area of the serpentine style is accounted for. The FOM will become 23606, simply the best of all.

5 Future Enhancement

The proposed OSC is a prototype for verifying the layout arrangement impact on CMOS oscillators. Thus, the main issue to be improved in the future is to enlarge the frequency range.

6 Conclusion

This investigation presents detailed analysis of OSC layout styles to conclude that the serpentine layout significantly reduces the variation impact. Moreover, the proposed layout method can be used to other CMOS processes. The proposed serpentine layout style can be applied in other CMOS technology nodes to make the chip performance more predictable in the early design stage.

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